

Experiment No.

Date: / / 20....

TO DETERMINE THE ACCELERATION DUE TO GRAVITY IN THE LABORATORY BY USING A SIMPLE PENDULUM AND HENCE DETERMINE THE LENGTH OF SECOND PENDULUM BY THE HELP OF GRAPH BETWEEN T Vs L AS WELL AS T^2 Vs L .

APPARATUS REQUIRED:

- 1. A pendulum bob
- 2. A thread (about 1.5m)
- 3. A vernier calliper
- 4. A stop watch
- 5. A stand with clamp
- 6. A meter scale

THEORY:

A simple pendulum consists of a small metal ball (called bob or mass) suspended from a fixed point by a long thread such that the bob is free to swing back and forth in a vertical plane under the influence of gravity.

The oscillation of simple pendulum is simple harmonic for small angular displacement ($\theta < 6^\circ$).

Effective length of simple pendulum:

The distance between the point of suspension and center of gravity (CG) of the bob is called as effective length of simple pendulum.

Expression for time period of simple pendulum:

The restoring force acting on the pendulum at point B is:

$$F = -mg \sin\theta$$

or, $ma = -mg \theta$ [\because for small θ , $\sin\theta \approx \theta$]

or, $a = -g \theta$

or, $a = -g \frac{y}{L}$ [$\because \theta = \frac{\text{Arc } AC}{L} \approx \frac{y}{L}$]

or, $a = -\frac{g}{L} y$ (1)

or, $a \propto -y$

This shows that the motion of simple pendulum under small displacement is simple harmonic.

For a simple harmonic oscillator,

$$a = -\omega^2 y \dots \dots \dots (2)$$

On comparing equations (1) and (2), we get

$$\omega^2 = \frac{g}{L}$$

or, $\omega = \sqrt{\frac{g}{L}}$

or, $\frac{2\pi}{T} = \sqrt{\frac{g}{L}}$

or, $T = 2\pi \sqrt{\frac{L}{g}}$

This is the expression for time period of oscillation of simple pendulum.

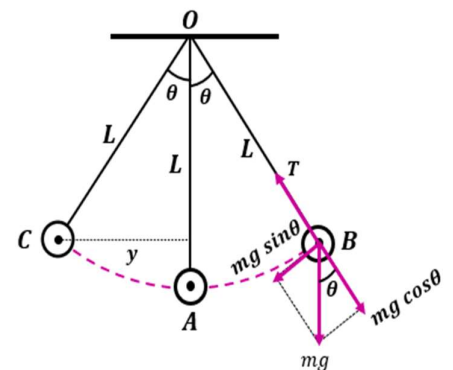


Figure: Oscillation of simple pendulum

Note:

$$T = 2\pi \sqrt{\frac{L}{g}}$$

- L = effective length of simple pendulum
- g = effective acceleration due to gravity

$$\therefore T = 2\pi \sqrt{\frac{L_{eff}}{g_{eff}}}$$

Example:

- ✓ For a lift under free fall, $g_{eff} = 0$.
- ✓ For a satellite, $g_{eff} = 0$.

Hence, time period of oscillation of simple pendulum in above cases is **infinite**.

(The pendulum does not swing at all).

❖ The time period of simple pendulum is **independent of:**

- 1. Mass of the pendulum.
- 2. Amplitude of oscillation.