

10. Linear momentum (P) = $mv = [M][LT^{-1}] = [MLT^{-1}]$

11. Gravitational constant (G) = $\frac{Fr^2}{Mm} = \frac{[MLT^{-2}][L^2]}{[M^2]} = [M^{-1}L^3T^{-2}]$

12. Specific Heat Capacity (S) = $\frac{Q}{m\Delta\theta} = \frac{[ML^2T^{-2}]}{[M][K]} = [M^0L^2T^{-2}K^{-1}]$

13. Power (P) = $\frac{work(W)}{time(t)} = \frac{[ML^2T^{-2}]}{[T]} = [ML^2T^{-3}]$

Quantities Having Same Dimensions

- ✓ $[M^0L^0T^{-1}]$ = Frequency, angular frequency, angular velocity, velocity gradient.
- ✓ $[M^1L^2T^{-2}]$ = Work, energy, P.E, K.E, torque, moment of force
- ✓ $[M^1L^{-1}T^{-2}]$ = Pressure, stress, young's modules (stress/Strain), bulk modulus (Pressure/fraction change in volume), modulus of rigidity (Force/Area), energy density
- ✓ $[M^1L^1T^{-1}]$ = Momentum, Impulse
- ✓ $[M^0L^1T^{-2}]$ = g, gravitational field intensity
- ✓ $[M^1L^1T^{-2}]$ = Thrust, force, weight, energy gradient
- ✓ $[M^1L^2T^{-1}]$ = Angular momentum, plank's constant

Dimensionless quantities:

- ✓ **Strain, Refractive index, Relative density (Specific Gravity), Angle, Solid Angle, exponential term, Trigonometric functions**

- ✓ Numerical constants, trigonometric functions, exponential functions, logarithmic functions have no dimension - $[M^0L^0T^0]$.
- ✓ Some quantities may have unit but no dimension. For example: plane angle (unit: rad), solid angle (unit: Sr).

Principle of Homogeneity:

It states that “only the physical quantities having the same dimensions can be added or subtracted. For a correct physical equation, the dimensions on LHS and RHS are always the same.” i.e.: $A + B + C = 0$,

$$\text{Dimension of } A = \text{Dimension of } B = \text{Dimension of } C$$

Example:

In an equation: $v = u + at$, the dimension of v , u and at must be the same.

Problem: The force F is given in terms of time (t) and displacement(x) by the equation $F = A \sin Bx + C \sin Dt$. What is the dimension of A , B , C , D , and D/B ?

Solⁿ:

From principle of homogeneity,

$$[F] = [A \sin Bx] = [C \sin Dt] \dots \dots \dots (1)$$

Where, $[\sin Bx] = [M^0L^0T^0]$.

$$[\sin Dt] = [M^0L^0T^0]$$

$$[Bx] = [M^0L^0T^0]$$

$$[Dt] = [M^0L^0T^0]$$