

Now, simplifying equation (1) in dimensional form, we get,

$$[M^1L^1T^{-2}] = [A] = [C]$$

Next,

Since, $[Bx] = [M^0L^0T^0]$

Or $[B] [x] = [M^0L^0T^0]$

Or $[B] = \frac{[M^0L^0T^0]}{[M^0L^1T^0]}$; x is displacement

$$\therefore [B] = [M^0L^{-1}T^0]$$

And

Since, $[Dt] = [M^0L^0T^0]$

Or $[D] [t] = [M^0L^0T^0]$

Or $[D] = \frac{[M^0L^0T^0]}{[M^0L^0T^1]}$; t is time

$$\therefore [D] = [M^0L^0T^{-1}]$$

Finally,

$$\left[\frac{D}{B}\right] = \frac{[M^0L^0T^{-1}]}{[M^0L^{-1}T^0]} = [M^0L^1T^{-1}]$$

The corresponding unit is ms^{-1} and the corresponding quantity is speed or velocity.

Check Yourself:

1. The velocity v of a particle depends on time t as $v = At^2 + Bt + C$ where v is in m/s and t is in second. What are the units of A , B and C?
2. If $y = a + bt + ct^2$, where y is displacement and t is time. What are the dimensions of a , b and c ?
3. Van der Waal's equation of state is: $\left(P + \frac{a}{V^2}\right)(V - b) = RT$ where P is pressure, V is volume, T is temperature and R is universal gas constant. Find the dimensions of Vander Waal's constants a and b . Also prove that the dimensions of $\frac{a}{b}$ are same as those of work.
4. Find the dimension of a and b in equation $p = ae^{bt}$, where, p is pressure, and t is time.
5. The force F is given in terms of time (t) and the displacement (x) by the equation:

$$F = A\cos Bx + C\sin Dt. \text{ Find the dimension of } \frac{D}{B} \text{ and } \frac{A}{C}.$$

Uses (or application) of dimensional analysis:

1. To convert one system of units into another system.
2. To check the correctness of a physical relation (checking a formula).
3. To establish the relation between various physical quantities (finding a formula).
4. To find the dimension of constants in a given relation.

Uses 1:

To convert one system of units into another system.

Dimensional analysis is used to find the relationship between two units of a physical quantity in two different systems.

For example, the SI unit of force is Newton N, and the CGS unit of force is dyne.