

Hence, $\phi = \frac{2\pi}{\lambda} \times x$

Or $\phi = kx \dots \dots \dots (3)$

Using equation (3) in equation (2), we get

$y = a \sin(\omega t - kx) \dots \dots \dots (4)$: Equation of plane progressive wave.

Note:

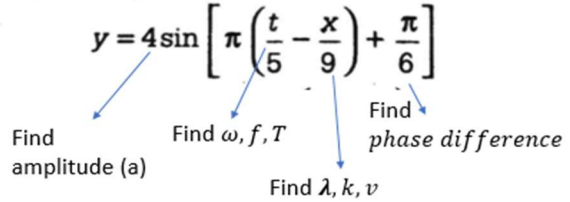
Wave equation could be of the form:

$y = a \sin[(\omega t \pm kx) \pm \phi]$

❖ In the given wave equation, find:

1. Amplitude
2. Angular frequency, frequency and time period
3. Wavelength, propagation constant (angular wave number) and wave velocity
4. Phase difference
5. Initial phase.

In the wave equation like:



Principle of superposition:

Statement:

When a large number of waves are travelling **simultaneously** through a medium, the resultant displacement of a particle at any point is equal to the **vector sum** of displacements produced by each individual wave.

If $y_1, y_2, y_3, \dots \dots \dots$ are the displacements at a point due to different waves independently and if those waves travel simultaneously through the point, then the resultant displacement (y) of the point is:

$\vec{y} = \vec{y}_1 + \vec{y}_2 + \vec{y}_3 + \dots \dots \dots$

In magnitude,

$y = y_1 + y_2 + y_3 + \dots \dots \dots$

1. Two identical sinusoidal waves each of amplitude 10 mm with a phase difference of 90° are travelling in the same direction in a string. The amplitude of the resultant wave is
 a. 5 mm b. $10\sqrt{2}$ mm c. 10 mm d. 20 mm
2. The displacement of an elastic wave is given by the function $y = 3 \sin \omega t + 4 \cos \omega t$, where y is in cm and t is in sec. The resultant amplitude is
 a. 3 cm b. 4 cm c. 5 cm d. 7 cm
3. Two waves produced displacement at a point given by: $y_1 = a \sin \omega t$ & $y_2 = a \sin(\omega t + \pi/2)$. The resultant amplitude is:
 a. 0 b. $2a$ c. $\sqrt{2}a$ d. $a/\sqrt{2}$

Applications of principle of superposition in wave phenomena:

1. In the formation of stationary wave
2. In the interference of waves
3. In the diffraction of waves
4. In the formation of beats etc.