

Let,  $\vec{F}_{AB}$  be force on body 'A' due to body 'B' and  $\vec{F}_{BA}$  be force on body 'B' due to body 'A' (during collision), Then from newton's 2<sup>nd</sup> law of motion,

$$\vec{F}_{AB} = \frac{\text{Change in momentum of A}}{\text{time}}$$

$$\therefore F_{AB} = \frac{m_1 v_1 - m_1 u_1}{t} \text{ --- (1) (Action)}$$

Similarly,

$$F_{BA} = \frac{m_2 v_2 - m_2 u_2}{t} \text{ --- (2) (Reaction)}$$

Next, from Newton's 3<sup>rd</sup> law of motion,

$$\vec{F}_{AB} = -\vec{F}_{BA} \text{ ; } -ve \text{ sign indicated the opposite direction}$$

$$\text{or, } \frac{m_1 v_1 - m_1 u_1}{t} = -\frac{m_2 v_2 - m_2 u_2}{t}$$

$$\text{or, } m_1 v_1 - m_1 u_1 = -m_2 v_2 + m_2 u_2$$

$$\therefore m_1 u_1 + m_2 u_2 = m_1 v_1 + m_2 v_2$$

**Therefore,**

$$\textbf{Total momentum before collision = Total momentum after collision}$$

Thus, the principle of conservation of linear momentum is verified using Newton's 2<sup>nd</sup> and 3<sup>rd</sup> laws of motion.

- *In the absence of net external force, the total momentum before the collision is equal to the total momentum after the collision.*

Simplified Note